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Optimal Wavelet Basis for Wavelet Packets based Meningioma Subtype Classification

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Abstract. Wavelets based analysis has been used frequently in literature for texture analysis and features extraction. Due to the availability of many wavelet filters, the issue of the selection of the optimal filter for a certain problem has always been an interesting research problem. In this paper, we present a study and comparative analysis of various wavelet filters for the problem of texture classification. The results are quite interesting as they identify wavelet properties that are desirable for wavelet based textural analysis and classification of meningioma subtypes.

1 Introduction

Meningiomas are tumours of the brain and nervous system. The problem of meningioma subtype classification essentially involves discriminating between four different subtypes of meningiomas, each having distinct characteristics and at the same time many dissimilar textural properties. Meningiomas account for 20% of all brain tumours and exist in three different grades of malignancy (WHO Grad I-III), most being benign (over 80%), but some showing an increased propensity to recurrence and rare cases being malignant. Most benign WHO Grade I meningiomas belong to one of the subtypes shown in Figure 1.

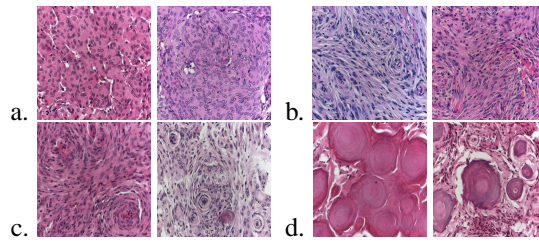


Figure 1. Meningioma Images for each subtype a. Meningiothelial (cells form syncytium), b. Fibroblastic (spindle shaped cells in collagen-rich matrix), c. Transitional (cells form whorls with psammoma bodies), d. Psammomatous (high number of psammoma bodies)

Histopathological diagnosis of tumours, especially of the brain and spinal cord, requires decision making by human experts. Visual diagnosis and decision making are hampered by two limitations: First, reviewing histological slides by humans is time consuming and the human experts are not always available. Secondly, although a lot of effort has been made to exactly define diagnostic criteria for all tumour entities within the World Health Organization (WHO) Classification of Tumours [1], the inter-rater variability is still considerable (see e.g. [2]). This consequently influences further therapy regimens greatly and hence a bias is introduced. Due to the progress in digital image retrieval and analysis technologies, machine based decision making may be used to support histopathologists by providing more objective diagnostic parameters and allow for high-throughput analysis. In our work, we are aiming to develop machine based texture analysis techniques for texture classification. The figure 1 shows two samples of each the meningioma subtypes indicating the variability in the textures and also the fact that the colour information is not useful. Hence, the problem is more complex than a general texture classification problem.

Our previous work in the area has shown promising results as per the classification accuracy achieved using a wavelets packet based transform technique called Adaptive Discriminant Wavelet Packets Transform (ADWPT) [3] [4]. Lessman et. al. [5] have shown that simple wavelet transforms are useful in acquiring features for pattern association. Transform techniques have been used frequently in literature for feature extraction for pattern classification. Unser et. al. [6] [7] have shown wavelet transforms to be powerful techniques for pattern classification. Gabor wavelet transforms have been shown to be more effective than other techniques for texture classification [8,9]. In all transform based techniques, the issue of selection of the appropriate subbands is of paramount importance. Saito and Coifman [10] employed wavelet packet transform for optimal local features extraction using relative entropy as the criterion for basis selection. Rajpoot [11] developed discriminant wavelet packets for optimal subband selection for texture classification. On these

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lines we have developed the ADWPT, the details of which could be found in our papers [3,4]. Another important issue is the selection of the appropriate filter for texture classification. In the domain of compression a lot of work in optimal filter selection has been carried out [12] [13]. Similarly some effort has been expended in defining which filters are optimal for features extraction in the domain of texture classification. Some interesting work in the area was carried out by Mojsilovic et. al. in defining which characteristics in a wavelet are useful for texture characterization [14]. In this paper, we try to ascertain which wavelets are optimal in our wavelet packets (ADWPT) based approach for meningioma subtype texture classification.

2 Methods

The methodology employed in this paper consists of the following steps.

1. Computation of a Full Wavelet Packet Transform using a wavelet filter.
2. Computation of the best basis i.e. the optimal set of subbands for discriminating between textures being studied.
3. Calculation of textural features from each subband.
4. Classification of textures based upon these textural features using Support Vector Machines (SVM).

2.1 Full Wavelet Packet Transform (FWPT)

The wavelet transform is computed by applying a highpass and lowpass filter upon the input signal to acquire the high frequency and low frequency subbands. A simple wavelet transform decomposes only the low level frequencies iteratively, whereas wavelet packets decomposes, all subbands. The wavelet packet decompositions are maintained in a quadtree structure, with the parent being the original subband or image and the children being the wavelet decompositions of the parent. A FWPT involves the decomposition of all the subbands up to a certain level whereas a simple wavelet transform only decomposes the approximation subband. The decomposition of the details at each level is done to extract relevant information. An overcomplete set of subbands is obtained with a lot of redundancy. An optimal subset has to be extracted from these.

2.2 Adaptive Discriminant Wavelet Packet Transform Algorithm

The next stage is the selection of the best basis or pruning of the tree. Before pruning can be done, the discrimination power of each subband must be computed. First, a pseudo probability density function (ppdf) is obtained for each subband using the normalized energy for the subband coefficients. A ppdf is computed by dividing the squares of a coefficient by the sum of the squares of the coefficients in a subband and is given by.

$$s_{m,n} = (x_{m,n})^2 / \sum_{i=0}^M \sum_{j=0}^N x_{i,j}^2$$

where $M \times N$ is the size of the subband, $s_{m,n}$ is the ppdf of the coefficient $x_{m,n}$ located at indices (m, n) of the subband. Next we compute the pseudo average probability density functions (papdf) by iteratively taking the pairwise average of the training images. It is important to note that these are computed for each class separately:

$$\mathcal{A}_{m,n}^{a_i} = (\mathcal{A}_{m,n}^{a_{i-1}} + s_{m,n}^{a_i})/2$$

where $s_{m,n}^{a_i}$ is the ppdf of the (m, n) th coefficient in a subband for the training image a_i belonging to class a . The process is repeated for all the subbands of the training images. It is important to note that an average of two subbands is computed per iteration. The objective is to acquire a basic model of probability distribution values for each class so that the difference between the classes may be estimated. This averaging is to be referred as pseudo averaging as it is different from the simple averaging. This is done to account for any sudden rise or falls in the probability distribution estimates. The pairwise discriminating power of the (p, q) th subband located at depth d is calculated using the Hellinger distance as follows:

$$\mathcal{D}_{d,p,q}^{c_i, c_j} = \sum_m^{M-1} \sum_n^{N-1} (\sqrt{\mathcal{A}_{m,n}^{c_i}} - \sqrt{\mathcal{A}_{m,n}^{c_j}})^2$$

where $\mathcal{A}_{m,n}^a$ and $\mathcal{A}_{m,n}^b$ denote the final average pseudo pdf's of the (m, n) th coefficient of the (p, q) th subband at depth

d for classes c_i and c_j respectively. This distance is calculated pairwise as indicated. So for a four class problem 6 such distances are computed. Subsequently the calculation of the overall discriminatory power \mathcal{P} is computed as,

$$\mathcal{P}_{d,p,q} = \sum_{i=1}^{n-1} \sum_{l=i+1}^n \mathcal{D}_{d,p,q}^{c_i, c_l}$$

where i and l represent the different class indices, p, q represents the subband number at depth d and n is the total number of classes. The process is repeated for all the subbands at various levels in the full wavelet packet decomposition. The next stage is the best basis selection.

2.2.1 Best Basis Selection

The algorithm for the best basis selection is stated below.

1. Compute the J -level full wavelet packet tree decomposition.
2. Calculate the discrimination power of each subband based upon the procedure described above.
3. Initialize $d = J - 1$.
4. For all $0 \leq p < 2^j, 0 \leq q < 2^j$, do the following:
 - a If $\mathcal{P}_{d,p,q} < \max[\mathcal{P}_{d+1,p,q}, \mathcal{P}_{d+1,p,q+1}, \mathcal{P}_{d+1,p+1,q}, \mathcal{P}_{d+1,p+1,q+1}]$ keep the four child subbands at depth $d + 1$ where $\mathcal{P}_{d,p,q}$ represents the discrimination power of a node at position p, q
 - b otherwise keep the parent at depth d and remove the child subbands.
5. Decrement d by 1.
6. If $d < 0$, then stop, otherwise goto step 3.

2.2.2 Best Basis Stability and Most Probable Decompositions

The best basis changes by 20% when the test and training data are changed. This means that when certain patients' data are excluded from the computation, the best basis obtained is different from the one when it is included. Hence, we did an analysis of all the data computing the best basis for all the different permutations (different test/training data sets) to acquire the most probable subbands i.e. the subbands that are selected most frequently. The results showed that most subbands were decomposed more than 80% of the time and there were very few occasions when the decomposition was different from the most probable subband. Hence, it was concluded for the given application that the most probable decomposition included the most useful subbands for a given filter. Figure 2.2.2 shows the decompositions obtained for some of the filters indicating the variability in the decompositions. The blue number indicates the subbands' discrimination power when subbands are ordered based upon their discrimination power. So the number 1 indicates that this is the most discriminant band. The magenta number indicates the percentage of how frequently this subband is obtained in the various test/training trial decompositions.

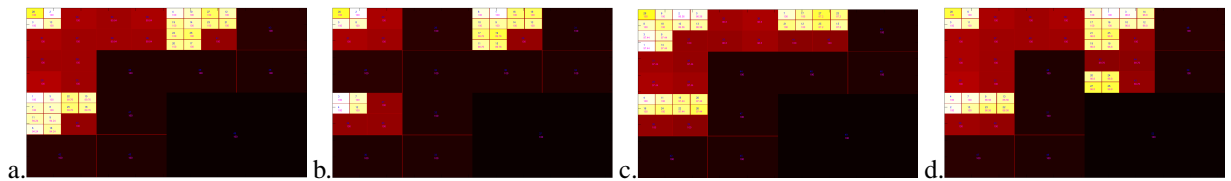


Figure 2. Most probable decompositions using various wavelet filters a.Coiflet-2 b.Biorthogonal4.4 c.Reverse biorthogonal 2.8 d.Daubechies-4

2.2.3 Best Basis and Features Extraction

Once the most discriminant subbands from the best basis are obtained, the next stage is the extraction of the gray level co-occurrence matrix (GLCM) features. The GLCM features employed were contrast, correlation, energy and homogeneity. The use of GLCM features with the ADWPT allows us to perform spatial analysis on the ADWPT subbands. We are able to exploit the spatial correlation inherent in the texture for classification purposes. GLCMs are

aided by the fact that high frequency resolution is obtained through ADWPT, which means that only a certain range of frequency coefficients is analysed at each subband level. The GLCM is computed over each subband. The Gray Level Co-occurrence Matrix C over a subband I , parameterized by an offset $(\Delta x, \Delta y)$ is defined by the formulae:

$$C_{ij} = \begin{cases} 1 & \text{if } I(p, q) = i \text{ and } I(p + \Delta x, q + \Delta y) = j \\ 0 & \text{otherwise} \end{cases}$$

Next, features for the GLCM, C_{ij} , are computed: Contrast($\sum_{i,j=0}^{N-1} C_{ij}(i-j)^2$) Correlation($\sum_{i,j=0}^{N-1} C_{ij} \frac{(i-\mu)(j-\mu)}{\sigma^2}$) Energy($\sum_{i,j=0}^{N-1} (C_{ij})^2$) Homogeneity($\sum_{i,j=0}^{N-1} \frac{C_{ij}}{1+(i-j)^2}$), where μ and σ represent the mean and standard deviation of the coefficient in the subband I . It can be seen from the equation that certain row (Δx) and column (Δy) offsets must be set. In our work, at present instance the row offset is set to 0 and the column offset is set to 1. Each feature has its own significance. Contrast measures the difference or the gradient in coefficient values over a subband. Correlation determines the relationship in terms of how the coefficients texture varies over a subband. Energy is a measure of non zero coefficients or the presence of texture in a subband. Homogeneity reflects the degree of similarity of the texture over a subband. Each of these features capture a certain spectral property of the texture.

2.2.4 Classification using Support Vector Machines

SVM is a supervised classifier, which approximates the decision surfaces of the theoretical Bayes classifier. SVM has found a broad area of application since its invention in 1995 by Vapnik [15]. SVM uses various kernels to map the input space into a higher dimensional feature space to make the non-linear hyperplane linear. To achieve this without increasing computational complexity a kernel is employed. The kernel function $K(x_i, x_j)$ computes an equivalent kernel value in the input space such that no explicit mapping is required. The Matlab version of LibSVM provided by Chang and Lin [16] was used in our analysis.

3 Results

The classification accuracies for various filters are presented in the table 1. The decompositions for each kind of wavelets was computed up to four levels. The GLCM features of contrast, correlation, energy and homogeneity are concocted together and used for training and testing of SVM. Each of the results have been cross-validated using 5 different test trial runs.

4 Conclusion and Discussion

A wavelet filter could be thought of as a microscope to analyse signals at various frequency and spatial resolutions. Hence, each kind of wavelet could be used to analyse a different aspect of a signal as they have different properties. This can be seen from our results in table 1, where certain filters perform better than others. Furthermore, some filters are seen to have better classification accuracy for one meningioma subtype, for instance, Coiflet-2 is better at classifying meningiotheliamatous and psammomatous meningiomas, whereas Daubechies-4 is better at classifying fibroblastic, psammomatous and transitional.

It can be seen here that the classification accuracies are not as high as the ones quoted in our previous work [4]. The reason for this is that rather than only applying contrast feature (optimal overall accuracy of 82%), four GLCM based features are used for classification. They bring robustness to our analysis by improving accuracies over all the different meningioma subtypes but bring down the overall classification accuracy. The objective of this paper is to analyze the effect of various filters on classification accuracy in order to acquire the best wavelet. The table shows that wavelet filters with certain characteristics are more useful for classification than others. From our results it could be safely concluded that regularity and orthogonal analysis are useful wavelet properties for image analysis and classification. Mojsilovic et. al. [14] in their analysis with the simple wavelet transform found biorthogonality and higher number of vanishing moments useful properties. Symmetry is not an important property as far as classification is concerned. In our analysis, assymetrical filters such as Daubechies 4 provides the best overall classification accuracy of 78%. Symmetrical wavelet coiflet 2 performs equally well with providing high classification accuracies for meningiotheliamatous which is one of the more difficult textures to classify. This paper dealt with mainly the effect of the use of different wavelets on classification accuracies. Comparison of wavelets with other techniques will be the subject of our future work.

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Table 1. Cross validated classification results for meningiomas (F=Fibroblastic, M=Meningiotheliomatous, P=Psammomatous, T=Transitional) for ADWPT features

Wavelets Filter	No. Features	<i>F</i>	<i>M</i>	<i>P</i>	<i>T</i>	Average
Haar	13X4	68	55	88	35	61
Symlets 5	40X4	70	65	96	78	77
Coiflet 2	49X4	56	90	98	69	78
Daubechies 5	46X4	59	68	93	69	72
Biorthogonal 4.4	42X4	59	64	94	61	69
Reverse biorthogonal 2.8	49X4	63	54	93	74	71
Daubechies 4	52X4	77	63	98	75	78
Daubechies 10	64X4	74	62	91	58	71
Symlets 10	37X4	60	72	92	75	75
Reverse biorthogonal 1.3	34X4	60	58	94	58	67
Reverse biorthogonal 3.9	58X4	69	50	95	71	71
Biorthogonal 2.4	40X4	61	51	94	56	66
Biorthogonal 6.8	46X4	63	73	96	70	75
Reverse biorthogonal 2.4	43X4	58	50	96	71	69
Reverse biorthogonal 4.4	46X4	61	55	96	66	70
Coiflets 1	49X4	61	51	95	62	68
Biorthogonal 1.5	13X4	55	52	88	38	58
Reverse biorthogonal 3.1	40X4	58	78	86	55	69
Reverse biorthogonal 1.5	42X4	69	71	94	58	73
Symlets 6	46X4	70	56	94	59	70
Reverse biorthogonal 6.8	43X4	64	70	91	77	74
Symlets 9	46X4	68	59	91	69	72
Biorthogonal 2.8	43X4	65	62	96	59	71
Biorthogonal 3.9	55X4	76	66	91	54	72

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